

A Novel Multi-Level Privacy Preserving Public Auditing Scheme for Cloud Data Sharing with Multiple Managers

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Abstract

Today, cloud storage becomes one of the critical services, because users can easily modify and share data with others in cloud. However, the integrity of shared cloud data is vulnerable to inevitable hardware faults, software failures or human errors. To make sure the integrity of the shared data, some schemes have been invented to allow public verifiers (i.e., third party auditors) to efficiently audit data integrity without retrieving the entire users' data from cloud. Unfortunately, public auditing on the integrity of shared data may reveal data owners' sensitive information to the third party auditor. In this paper, we suggest a new privacy-aware public auditing mechanism for shared cloud data by establishing a homomorphic verifiable group signature. Unlike the existing solutions, our scheme requires at least t group managers to recover a trace key cooperatively, which eliminates the abuse of single-authority power and provides non-frameability. Moreover, our scheme make sure that group users can trace data changes through designated binary tree; and can recover the latest correct data block when the current data block is damaged. Moreover, the formal security analysis and experimental results show that our scheme is sustainably secure and cost-effective.

Index Terms — Data Integrity; Homomorphic Verifiable; Nonframeability; Provable Security.

I. INTRODUCTION

Due to the increasing number of applications of shared data, such as iCloud, Google Docs, and so on, users can upload their data to a cloud and share it with other peers as a group. Unfortunately, since cloud servers are vulnerable to inevitable hardware faults, software failures or human errors, data stored in the cloud may be spoiled or lost. In the worst cases, a cloud owner may even conceal data error accidents in

order to preserve its reputation or avoid profit losses. In addition, users who lose direct control over their data are not sure whether their cloud-stored data is intact or not. Therefore, integrity verification for the shared data in the cloud is an important, yet timely issue for a large number of cloud users. To ensure the integrity of data stored in cloud servers, a number of mechanisms based on various techniques have been proposed. In particular, in order to minimize the responsibility on users, a trusted third-party auditor (TPA) is occupied to manage the verification, which is called public auditing. However, the TPA may have unnecessary access to private information during the auditing process. Therefore, researchers proposed some new schemes to protect privacy, including data privacy, and identity privacy. To be particular, the TPA cannot acquire each block that is authorized by a particular user in the group by establishing homomorphic authenticable ring signatures or computing tags based on ordinary group private key. However, since both methods concern about unconditional privacy, the real identity of the signer can no longer be traced. A later development is the homomorphic authenticable group signature scheme based on group signatures, which is designed to protect privacy. On one hand, the identity of each signer is anonymous; and on the other hand, the group manager can trace a signer's real identity after a dispute. Regrettably, in all surviving public auditing schemes, the detecting process is trained by a single entity. As a result, that entity has the privilege of tracing, which may lead to abuse of single-authority power. Therefore, an innocent user may be framed or a malicious user may be harbored.

Meanwhile, to support data dynamics, the data structure based on index hash table or Merkle Hash Tree (MHT) has been utilized. However, this kind of data structure merely records the newest data block with the corresponding signature, which prevents users from tracing the changes of the data blocks. When the current data has been corrupted, users cannot recover the old

data from the records. Therefore, the problem of data traceability and recoverability also should be considered.

Moreover, a necessary authentication process is missing between the auditor and the cloud in most existing public auditing schemes, hence anyone can challenge the cloud for the auditing proofs. This problem will trigger network congestion and unnecessary waste of cloud resources. Although Liu et al. designed an authorized public auditing scheme to solve the problem, it is only suitable for a single client, and cannot be applied to group-shared data. Since the malicious or pretended auditors/users might constantly request cloud access for the auditing proof by utilizing TPA, unauthorized auditing is another important issue that should be addressed in integrity verification for shared cloud data.

At present, all the existing public auditing schemes only consider a single group manager when applied to shared data with group users. However, in real-world applications, there might be multiple managers in a group. For instance, the shared data of a project team is created by multiple managers together, what's more, any of them can maintain the shared data. Another important practical problem is that the group users should be able to dynamically enroll and revoke the group, which will be managed by the group managers. And significantly, when tracing the real identity of the signer, a specified number of managers can work together, which ensures the fairness of the tracing process.

In this paper, we propose a new privacy-aware public auditing mechanism, called NPP, for the shared cloud data with multiple group managers. Our contributions can be summarized as follows.

1) We construct a model for data (in a group) divided with numerous group managers, and suggest a new privacy preservation public auditing scheme for numerous group managers in shared cloud storage. Our proposed scheme can not only provide multi-levels privacy-preservation abilities (including identity privacy, traceability and non-frameability), but also can well support group user revocation.

2) We design a data structure based on a binary tree for clouds to record all the changes of data blocks. Group users can trace the data changes through the binary tree and recover the

latest correct data block when the current data block is damaged.

3) We utilize an authorized authentication process to verify TPA's challenge messages. Therefore, only the TPA who has been authorized by the group users can pass the authentication and then challenge the cloud, which protects clouds from malicious challenges.

4) Our formal security analysis and experimental results show that NPP is provably secure and efficient.

The rest of this paper is organized as follows. Section II presents a review of related work on public auditing schemes in cloud storage. Then we introduce our system model, threat model and design objectives in Section III. Section IV briefly introduces the cryptographic knowledge applied in our scheme. In Section V, we describe the proposed public auditing scheme NPP in detail and Section VI evaluates its performance. Finally, this paper is concluded in Section VII.

II. RELATED WORK

Ateniese et al. firstly proposed the Provable Data Possession (PDP) model, utilizing homomorphic verifiable tags, and the process of data integrity checking was a kind of "challenge-response" protocol. In order to support data retrievability, Juels et al. proposed the Proofs of Retrievability (POR) model.

Considering the application of cloud data shared by group users, Wang et al. proposed a privacy-preserving public auditing scheme, called Oruta, for shared data in the cloud. Their scheme was based on a homomorphic authenticable ring signature, which allows a public auditor to audit the shared data without retrieving all data from the cloud. However, the auditing raised dimensionally increases with the number of group users, hence it is not acceptable for large groups in the cloud. To support large groups, Wang et al. proposed a new auditing scheme, called Knox. The auditing overhead is independent of the number of group users, hence Knox can support shared data with large groups. Moreover, any group manager can reveal the identity of the signer. Unfortunately, the scheme cannot support user revocation.

In addition, to eliminate threats of unauthorized audit challenges from malicious or pretended third-party auditors, Liu et al. proposed

an authorized auditing scheme by adding an additional authentication process between the cloud and the TPA. Additionally, to support fine-grained update requests, the authorized scheme employed BLS signatures and MHT. However, the scheme can only be applied to a single client.

III. PROBLEM STATEMENT

In this part, we explain the system model and the threat model and give the design objectives of our public auditing scheme.

A. System Model

As shown in Fig. 1, the system model contains four entities: cloud, TPA, trusted private key generator (PKG), and group users. The cloud has powerful storage space and computing capacity, and provides services (e.g., data storage, data sharing, etc.) for group users. The TPA can verify the integrity of the shared data on behalf of the group users. The PKG generates the system public parameters and group key pair for group users. The group users include two types of users: GMs(Group Managers) and ordinary members.

Unlike existing system models, the GMs contain multiple members who create the shared data together and share them with the ordinary members through the cloud. Therefore, GMs operates as the common owners of the actual data, and their identities are equal. Meanwhile, any of the GMs can add new members or remove members from the group. In addition, either a GM or an ordinary member can access, download, and modify the shared data in the cloud. Note that multiple managers in a group is very common in practice. For instance, the shared data of a project team is created by multiple managers together. Later, any of the GMs can maintain the shared data and manage the group users. When tracing the real identity of the signer, a given number of managers can cooperate to detect the real identity, which ensures the integrity of the tracing process.

When a group user wants to check the integrity of the shared data, she/he first submits an auditing request message to the TPA. After receiving the request, the TPA challenges the cloud for an auditing proof. Once the cloud receives the auditing challenge, it firstly authenticates the TPA. If authentic, the cloud will give back the auditing proof to the TPA. Otherwise the cloud will refuse the request. Finally, the TPA verifies the validity of the proof and sends an auditing response to the group user.

B. Threat Model

1) **Integrity Threat.** There are two kinds of threats related to shared data integrity. One is that external attackers might corrupt the shared data in the cloud, so that group users can no longer access the correct data. The other is that the cloud may corrupt or delete the shared data due to the hardware/software faults or human errors. What's worse, the cloud may conceal the fact of data damage from users in order to maintain self-interest and service reputation.

2) **Privacy Threat.** As a trusted and inquisitive verifier, a TPA might obtain some privacy information from the verification metadata during the auditing process. For instance, the TPA might analyze which data block has been modified most or which user has modified the data most, and finally conclude which particular data block or which group user is of a higher value than the others. Then the TPA might directly obtain the data or the identity of the group user from the signatures of the data blocks.

3) **Challenge Threat.** Because the auditing challenge message is very simple and has not been authorized, any other entity can utilize the TPA to challenge the cloud for auditing proofs.

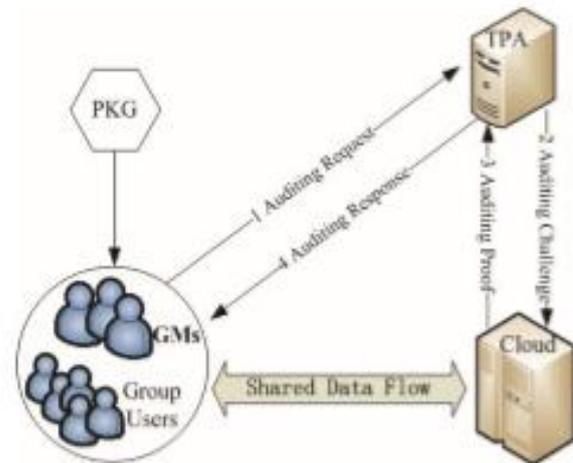


Fig. 1. The system model.

TABLE I
NOTIONS

Notions	Description
mpk	shared group public key
msk_t	the secret key of GM_t
$\{spk, ssk\}$	public/private key pair
usk_t	user signing key
upk_t	user membership key
rvk_t	user revocation key
$(V_{j,1}, V_{j,2}, \theta_j)$	the signature of the block m_j
$AUTH$	authorization
t	timestamp

In this case, a malicious entity might launch denial of service attacks on the cloud by sending massive challenge messages continuously, which will lead to network congestion and unnecessary waste of the clouds resources.

C. Design Objectives

To achieve integrity checking of the shared data in the cloud, NPP is expected to the following design objectives: **1) Public auditing:** Besides the group users, the TPA can also correctly check the integrity of the shared data in the cloud without retrieving entire users' data from cloud. **2) Authorized auditing:** Only the TPA that has been authorized by the group users can challenge the cloud. **3) Identity privacy:** During the process of auditing, the TPA cannot learn the identity of the group user from the signatures of the data blocks. **4) Traceability:** Under certain conditions, the group managers can reveal the signer's identity from the signatures and decide which group user has modified the data block. **5) Non-frameability:** Group managers can guarantee the fairness of the tracing process, i.e., innocent group user won't be framed and the misbehaved user won't be harbored by the group managers. **6) Support data traceability and recoverability:** Group users can easily trace the data changes and recover the latest correct data once current data is damaged. **7) Support group dynamics:** Group dynamics include two aspects. One is that GMs can easily join or leave the group, the other is that new users can be easily added into the group and misbehaved users can be efficiently excluded from the group.

IV. PRELIMINARIES

In this section, we briefly introduce the cryptographic knowledge applied in NPP. The main notations used in this paper are described in Table I.

A. Homomorphic Verifiable Tags

Homomorphic Verifiable Tags (HVTs) acting as the verification metadata of file blocks have been widely used in integrity checking for data stored in the cloud.

Definition (Homomorphic verifiable signature).

If an HVT based on signatures can satisfy the following two properties simultaneously, then the signature scheme is a homomorphic verifiable signature scheme.

Supposing (pk, sk) are the public/private key pair of the signer, σ_1 and σ_2 denote the tags of data block $m_1, m_2 \in Z_q$, respectively.

1) Blockless verification: A verifier can judge the correctness of all data through the linear combination of the data without retrieving it from the cloud. Specifically, given σ_1, σ_2 , two random numbers $y_1, y_2 \in Z_p$ and data block $m = y_1 m_1 + y_2 m_2$, a verifier can check the correctness of m without knowing m_1, m_2 .

2) Non-malleability: Any entity without the secret key cannot generate a new and valid tag through combining the known tags. Specifically, given σ_1, σ_2 , two random numbers $y_1, y_2 \in Z_p$ and data block $m = y_1 m_1 + y_2 m_2$, an entity who has no s_k cannot generate the valid tag σ for m by combining σ_1 and σ_2 .

B. Discrete Logarithm (DL) Problem

Definition (DL Problem).

Let $a \in Z_p^*$, given $g, g^a \in G_1$ as input, output a . The advantage of probabilistic polynomial time algorithm A in solving the DL problem in G_1 is defined as $\text{Adv}_{DL, A} = \Pr[A(g, g^a) = a : a \leftarrow_R Z_p^*]$, where the probability is over the choice of a , and the coin tosses of A . In this case, for any probabilistic polynomial time algorithm A , the advantage of solving the DL problem in G_1 is negligible.

V. THE NPP SCHEME

A. Overview

We assume that there is S group managers $GM_1 (1 < i \leq S)$ and d users $U_i (1 \leq i \leq d)$ in NPP. The shared data M is divided into w data blocks, i.e. $M = \{m_1, m_2, \dots, m_w\}$. In order to support dynamic operations on the shared data, we index each data block by leveraging index hash table. Specifically, NPP consists of eight algorithms: $\{Setup, Enroll, Revoke, Sign, Authorize, ProofGen, ProofVerify, Open\}$.

In *Setup phase*, the PKG sets parameters for the entire system, distributes the group key pair $\{mpk_1, msk_1\}$ and a shared public/private key pair $\{spk, ssk\}$ used to authorize each GM_1 , and initializes the membership information Ω . Then, any GM generates a user signing key usk_i , a (public) user membership key upk_i , and a user revocation key rvk_i for U_i . GM also shares the authorization key pair $\{spk, ssk\}$ with U_i in the *Enroll procedure*. Once a group user is revoked, GM invokes the *Revoke* algorithm to update Ω .

The group user can compute the signatures of the shared data block from the issued keys in the *Sign process*. With the *Authorize* algorithm, the group authorizes TPA to generate authorized auditing challenges, and then the valid TPA can check the integrity of the shared data on behalf of the group user. Once the cloud receives a challenge from TPA, the cloud verifies whether the challenge has been authorized and decides whether to generate the audit proof via *ProofGen*. TPA checks the correctness of the proof via *ProofVerify*. Finally, in the *Open* process, at least t GMs work together to trace the real identity of the signer.

B. Support Data Traceability and Recoverability

Since the identity of each data block can be described by the index hash table, i.e., $id_j = \{v_j, r_j\}$, where v_j is denoted as the virtual index of block m_j , and r_j is a random number generated by a collision-resistant hash function, every group



Fig. 2. The original records.

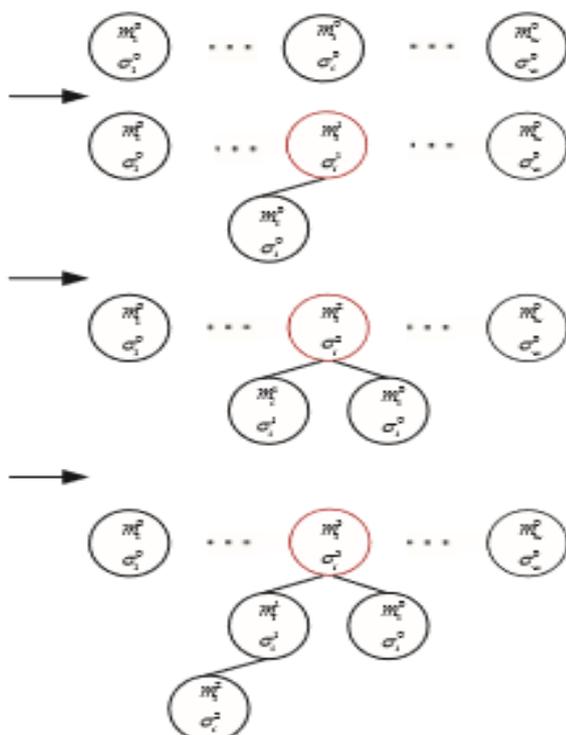


Fig. 3. The records when the i^{th} block has been updated three times

user can easily perform dynamic operations on the shared data, the details of which can be found in. However, if the data block has been changed maliciously, the group user cannot trace the changes and recover the right data.

To support data tracing and recovery, we have designed an additional data structure based on binary tree for the cloud server to record every change of data block. Through the records, group users can easily trace data changes. When the damaged has been found, group users can recover the right data by the records. As the group users can verify the older blocks one by one until discover the latest correct block. As shown in Fig. 2, original data block $\{m_1, m_2, \dots, m_w\}$ with the corresponding signatures $\{\sigma_1, \sigma_2, \dots, \sigma_w\}$ are stored as the roots of w binary trees respectively. $\{m_i^j, \sigma_i^j\} (1 \leq i \leq w)$ denotes the i th block has been modified j times, hence $\{m_i^0, \sigma_i^0\}$ means the data block is the original one. We will use some examples to show different records when group users

perform dynamic operations on the shared data later. Fig. 3 and 4 describe update operation and insert operation respectively. In addition, when group users want to delete a block, the cloud server still keeps the records related to this block, without any other additional operations. What's more, the cloud server does not need to know which block has been deleted.

As shown in Fig. 3, the i th block has been updated for three times, and the latest one is always the root of the binary tree; the old ones are the nodes of the binary tree. If we define the depth of the binary tree as N , then the number of nodes belongs to range $[2^{N-1}, 2^N - 1]$, and the number of times for the cloud to record the updates belongs to range $[2^{N-1} - 1, 2^N - 2]$.

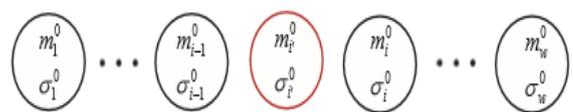


Fig. 4. The record when the block has been inserted.

When the current signature σ_3^i has been disfigured, group users can find the alterations $\{(m_2^i, \sigma_2^i), (m_1^i, \sigma_1^i), (m_0^i, \sigma_0^i)\}$ by applying the post-order traversal to the ultimate binary tree. As the disfigured signature cannot succeed in the verification, the group users are allowed to verify the signature σ_2^i , if it can succeed in the verification, then the newest right block has been established. If not, the group users remain verifying the signatures one at a time in proportion to the order of traversal tree with the help of TPA until the newest right block is found.

out. The verification algorithm can be found in the next section.

As shown in Fig. 4, when group users want to introduce a block, for example a new block m'_i is inserted between the block m_{i-1} and the block m_i , and $id'_i = \{v'_i, r'_i\} = \{\lfloor (v_{i-1} + v_i)/2 \rfloor, r'_i\}$, the cloud server will create a new root (i.e., $\{m_i^0, \sigma_i^0\}$) for this new block.

C. Construction of NPP

In this part, we explain the characteristics of the eight algorithms inserted. The data can be encrypted by the means of symmetrical encryption technology and attribute-based encryption technology before shared data is re-distributed to the cloud for protecting data privacy; however, this is outside the scope of our paper.

1) Setup: With the input security parameters $\varepsilon > 1$, $k, l_p \in \mathbb{N}$, PKG randomly selects parameters $\lambda_1, \lambda_2, \gamma_1$ and γ_2 such that $\lambda_1 > \varepsilon(\lambda_2 + k) + 2, \lambda_2 > 4l_p, \gamma_1 > \varepsilon(\gamma_2 + k) + 2$ and $\gamma_2 > \lambda_1 + 2$, two multiplicative cyclic groups G_1, G_2 with the same order q , and g_0 is the generator of G_1 . Then PKG selects a bilinear map $e : G_1 \times G_1 \rightarrow G_2$ and two oneway hash functions: $H_1\{0,1\}^* \rightarrow Z_q, H_2\{0,1\}^* \rightarrow G_1$, and defines two intervals: $A = [2^{\lambda_1} - 2^{\lambda_2}, 2^{\lambda_1} + 2^{\lambda_2}]$, $B = [2^{\gamma_1} - 2^{\gamma_2}, 2^{\gamma_1} + 2^{\gamma_2}]$. The parameters above are all public.

Then, PKG calculates the shared group public key $mpk = (n, a, a_0, Y, g_0, g, h, g_1, g_2, \eta_1, \eta_2)$ and each GM_i 's secret key $m_{sk}_i = (p', q', X_i)$ as follows:

- Select l_p -bit primes p', q' such that $P = 2p' + 1$, and $Q = 2q' + 1$. Set the modulus $n = PQ$ (Note that all the following arithmetic operations are modulo n unless specified otherwise).
- Select random elements $a, a_0, g, h, g_1, g_2, \eta_1, \eta_2 \in \mathbb{QR}(n)$ (of order q), where $\mathbb{QR}(n)$ denotes the set of quadratic residues of group Z_n^* .
- Select a random secret $X \in \mathbb{Z}_q^*$, and set $Y = g^X$.
- Select a $t-1$ degree polynomial $f(x) = b_0 + b_1x + \dots + b_{t-1}x^{t-1}$ with $b_0 = X, b_1, \dots, b_{t-1} \in \mathbb{Z}_q$, calculate $X_l = f(l) (l = 1, 2, \dots, S \text{ and } 2t - 1 \geq S)$, i.e. X is break up into S parts X_l [26].
- Initialize the membership information $\Omega = (c, u)$, where c is initialized to g_1 , and u is initialized to 1.

Next, PKG selects a public/private key pair $\{spk, ssk\}$ used for authorization (permission) only.

Finally, PKG sends $\{mpk, msk_i\}$ along with $\{spk, ssk\}$ to GM_i securely.

2) Enroll: The usk_i, rvk_i , and upk_i of a new member U_i are generated as follows:

- U_i generates a secret exponent $\tilde{x}_i \in \mathbb{R} [0, 2\lambda_2]$, a random integer $\tilde{r}_i \in \mathbb{R} [0, n]$, computes $C_1 = g^{\tilde{x}_i} h^{\tilde{r}_i}$ and broadcasts C_1 to any GM.
- GM who has received C_1 checks whether $C_1 \in \mathbb{QR}(n)$. If this is the case, the GM chooses $\alpha_i, \beta_i \in \mathbb{R} [0, 2\lambda_2]$ and sends $\{\alpha_i, \beta_i\}$ to U_i .
- U_i calculates $x_i = 2\lambda_1 + (\alpha_i \tilde{x}_i + \beta_i \text{ mod } 2\lambda_2)$, $C_2 = a^{x_i}$ and broadcasts C_2 to the GM.
- GM checks whether $C_2 \in \mathbb{QR}(n)$. If this is the case, GM selects $e_i, \pi \in \mathbb{R} B$, calculates $A_i = (C_2 a_0)^{1/e_i} = (a^{x_i} a_0)^{1/e_i}$, $\rho = g_0^\pi$ (ρ is public) and sends $\{A_i, e_i, \pi\}$ along with $\{spk, ssk\}$ to U_i .
- U_i checks $a^{x_i} a_0^{?} = A_i^{e_i}$. If the equation holds, U_i sets $usk_i = (x_i, \pi), rvk_i = e_i, upk_i = A_i$ and shares the key pair $\{spk, ssk\}$ with all the GMs.
- GM maintains a users-list, which contains all related keys and the valid time of the group users. Different users may be assigned with different valid times. Finally, GM adds U_i, U_i 's related keys and valid time to the list.

3) Revoke: Supposing user $U_k (1 \leq k \leq d)$ is to be revoked, the revocation key is rvk_k and the current membership information is $\Omega = (c, u)$, then any GM should update $c = c^{rvk_{k,u}} = c \cdot rvk_k$.

Suppose there are revoked users $\{U_e, \dots, U_k\} (1 \leq e < k \leq d)$, the latest $c = c^{\prod_{i=e}^{k} rvk_{i,u}} = \prod_{i=e}^k c^{rvk_i}$.

Then PKG distributes a new key pair $\{spk', ssk'\}$ to all GMs, and the GM shares it with the existing group users. Meanwhile, the GM updates the revoked users' valid time as a negative value in the users-list.

4) Sign: Group user U_i calculates the signature $\sigma_j = (V_{j,1}, V_{j,2}, \theta_j)$ for block $m_j \in \mathbb{Z}_q (1 \leq j \leq w, id_j \text{ is the identifier})$ as follows:

i. Compute $V_{j,1}$.

- Randomly select $r_j \in \mathbb{R} \{0, 1\}_{p}^{21}$ and calculate $T_{j,1} = Y_j^r A_j, T_{j,2} = g^r, T_{j,3} = g^{rvk_i} \cdot h^{r_j}$.

• Randomly select $r_{j,1} \in \mathbb{R} \pm \{0,1\}^{\varepsilon(\gamma_2+k)}$, $r_{j,2} \in \mathbb{R} \pm \{0,1\}^{\varepsilon(\lambda_2+k)}$, $r_{j,3} \in \mathbb{R} \pm \{0,1\}^{\varepsilon(\gamma_1+2lp+k+1)}$, $r_{j,4} \in \mathbb{R} \pm \{0,1\}^{\varepsilon(2lp+k)}$ and then calculate $d_{j,1} = T_{j,1}^{r_{j,1}} / (a_{j,2}^{r_{j,2}} \cdot Y_{j,3}^{r_{j,3}})$, $d_{j,2} = T_{j,2}^{r_{j,1}} / g_{j,3}^{r_{j,3}}$, $d_{j,3} = g_{j,4}^{r_{j,4}}$, $d_{j,4} = g_{j,1}^{r_{j,1}} \cdot h_{j,4}^{r_{j,4}}$.

• Calculate

$$v_{j,1} = \eta^{mj_1} H_1(g \| h \| Y \| a_0 \| a \| T_{j,1} \| T_{j,2} \| T_{j,3} \| d_{j,1} \| d_{j,2} \| d_{j,3} \| d_{j,4}).$$

• Calculate $s_{j,1} = r_{j,1} - v_{j,1}(rvk_i - 2^{\gamma_1})$, $s_{j,2} = r_{j,2} - v_{j,1}(x_i - 2^{\lambda_1})$, $s_{j,3} = r_{j,3} - v_{j,1} \cdot rvk_i \cdot r_j$, $s_{j,4} = r_{j,4} - v_{j,1} \cdot r_j$.

• Output

$$V_{j,1} = (v_{j,1}, s_{j,1}, s_{j,2}, s_{j,3}, s_{j,4}, T_{j,1}, T_{j,2}, T_{j,3}).$$

ii. Calculate $V_{j,2}$.

• Find $f, b \in \mathbb{Z}$ such that $f \cdot u + b \cdot rvk_i = 1$, and then set $d = g_1^{-b}$ (because U_i has not been revoked, rvk_i is not included in $u = \prod_{i=1}^k rvk_i$ and $\gcd(rvk_i, u) = 1$).

• Calculate $T_{j,4} = d \cdot g_{j,2}^{r_{j,2}}$.

• Randomly select $r_{j,5} \in \mathbb{R} \pm \{0,1\}^{\varepsilon(\gamma_2+k)}$, $r_{j,6} \in \mathbb{R} \pm \{0,1\}^{\varepsilon(\lambda_2+k)}$, $r_{j,7} \in \mathbb{R} \pm \{0,1\}^{\varepsilon(\gamma_1+2lp+k+1)}$, $r_{j,8} \in \mathbb{R} \pm \{0,1\}^{\varepsilon(2lp+k)}$ and calculate $d_{j,5} = T_{j,4}^{r_{j,5}} / (c_{j,6}^{r_{j,6}} \cdot g_{j,7}^{r_{j,7}})$, $d_{j,6} = g_{j,5}^{r_{j,5}} \cdot h_{j,8}^{r_{j,8}}$.

• Calculate

$$v_{j,2} = \eta^{mj_2} H_1(g \| h \| g_1 \| g_2 \| c \| T_{j,3} \| T_{j,4} \| d_{j,5} \| d_{j,6}).$$

• Calculate $s_{j,5} = r_{j,5} - v_{j,2}(rvk_i - 2^{\gamma_1})$, $s_{j,6} = r_{j,6} - v_{j,2}(f - 2^{\lambda_1})$, $s_{j,7} = r_{j,7} - v_{j,2} \cdot rvk_i \cdot r_j$, $s_{j,8} = r_{j,8} - v_{j,2} \cdot r_j$.

• Output $V_{j,2} = (v_{j,2}, s_{j,5}, s_{j,6}, s_{j,7}, s_{j,8}, T_{j,3}, T_{j,4})$.

iii. Calculate tag $\theta_j = [H_2(id_j)g^{mj_0}] \pi$.

iv. Output the signature $\sigma_j = (V_{j,1}, V_{j,2}, \theta_j)$.

5) **Authorize:** Any group member can authorize the TPA on behalf of the group to challenge the cloud through the shared key pair $\{spk, ssk\}$ as follows:

• The group member asks the ID of the TPA (for security, the ID is used for authorization only). Then the TPA returns its ID encrypted with the public key spk .

• The group member decrypts it with ssk to get ID, calculates $sig_{AUTH} = Sig_{ssk}(AUTH \| t \| ID)$ (AUTH means authorization and t is the timestamp), and sends sig_{AUTH} as the auditing authorization message to the TPA. Then the TPA can challenge the cloud on behalf of the group users.

Note that after message $\{AUTH, t, sig_{AUTH}\}$ is stored in the cloud along with the signatures of the data blocks, it will be deleted from local storage.

6) **ProofGen:** In this phase, the TPA first sends a challenge message to the cloud, and then the cloud generates an auditing proof message if the TPA is authorized.

i. The TPA challenges the cloud as follows:

• Randomly select a subset Γ from the set $[1, w]$, where Γ contains D elements, i.e. $|\Gamma| = D$.

• Generate random numbers $y_j \in \mathbb{Z}_q, j \in \Gamma$.

• Send an auditing challenge message $\{sig_{AUTH}, \{ID\}PK_{cloud}, \{(j, y_j)\}_{j \in \Gamma}\}$ to the cloud. Because the PK_{cloud} is the public key of the cloud, the cloud can decrypt $\{ID\}PK_{cloud}$ with the corresponding private key SK_{cloud} to get ID.

ii. The cloud checks whether the TPA has been authorized as follows:

• Calculate ID by decrypting $\{ID\}PK_{cloud}$ with its private key SK_{cloud} .

• Decrypt sig_{AUTH} with the group's public key spk to get ID, AUTH and t. If $ID = ID'$, the calculated AUTH is equal to the AUTH stored in the cloud and t is valid, the cloud will generate the auditing proof. Otherwise, the cloud will refuse to generate the proof.

iii. The cloud generates the auditing proof message to the TPA as follows:

• Calculate $\lambda = \sum_{i \in \Gamma} y_j m_j \in \mathbb{Z}_q$ and aggregate the selected tags as $\Theta = \prod_{j \in \Gamma} \theta_j^{y_j} \in G_1$.

• Output $\Phi_j = \{V_{j,1}, V_{j,2}\}_{j \in \Gamma}$ based on the selected blocks, where $V_{j,1} = (v_{j,1}, s_{j,1}, s_{j,2}, s_{j,3}, s_{j,4}, T_{j,1}, T_{j,2}, T_{j,3})$, $V_{j,2} = (v_{j,2}, s_{j,5}, s_{j,6}, s_{j,7}, s_{j,8}, T_{j,3}, T_{j,4})$.

• Send the auditing proof $\{\{id_j\}_{j \in \Gamma}, \{\Phi_j\}_{j \in \Gamma}, \lambda, \Theta\}$ to the TPA.

7) **ProofVerify:** The TPA checks the correctness of the proof as follows.

• Calculate $d'_{j,1} \sim d'_{j,6}$ as follows:

$$d'_{j,1} = (a_0^{v_{j,1}} \cdot T_{j,1}^{s_{j,1} - v_{j,1} \cdot 2^{\gamma_1}}) / (a^{s_{j,2} - v_{j,1} \cdot 2^{\lambda_1}} \cdot Y^{s_{j,3}}) \quad (1)$$

$$d'_{j,2} = T_{j,2}^{s_{j,5} - v_{j,1} \cdot 2^{\gamma_1}} / g^{s_{j,6}} \quad (2)$$

$$d'_{j,3} = T_{j,2}^{v_{j,1}} \cdot g^{s_{j,4}} \quad (3)$$

$$d'_{j,4} = T^{vj,1}_{j,3} \cdot g^{sj,1-vj,1 \cdot 2\gamma_1} \cdot h^{sj,4} \quad (4)$$

$$d'_{j,5} = ((g^{-1}_1)^{vj,2} \cdot T^{sj,5-vj,2 \cdot 2\gamma_2}) / (c^{sj,6-vj,2 \cdot 2\lambda_1} \cdot g^{sj,7}) \quad (5)$$

$$d'_{j,6} = T^{vj,2}_{j,3} \cdot g^{sj,5-vj,2 \cdot 2\gamma_1} \cdot h^{sj,8} \quad (6)$$

• Verify the correctness of the following equations:

$$\prod_{j \in \Gamma} v^{y_{j,1}} = \eta^{\lambda_1} \prod_{j \in \Gamma} H_1(g \| \dots \| d'_{j,4}) y_j \quad (7)$$

$$\prod_{j \in \Gamma} v^{y_{j,2}} = \eta^{\lambda_2} \prod_{j \in \Gamma} H_1(g \| \dots \| d'_{j,6}) y_j \quad (8)$$

$$e(\Theta, g_0) = e(\prod_{j \in \Gamma} H_2(id_j)^{y_j} \cdot g^{\lambda_0, \rho}) \quad (9)$$

Note that for simplicity, we use $H_1(g \| h \| \dots \| d'_{j,4})$ and $H_1(g \| h \| \dots \| d'_{j,6})$ instead of $H_1(g \| h \| Y \| a_0 \| a \| T_{j,1} \| T_{j,2} \| T_{j,3} \| d'_{j,1} \| d'_{j,2} \| d'_{j,3} \| d'_{j,4})$ and $H_1(g \| h \| g_1 \| g_2 \| c \| T_{j,3} \| T_{j,4} \| d'_{j,5} \| d'_{j,6})$, repetitively, in the following parts.

• If the equations (7) (8) (9) all hold, then the auditing proof is valid. Otherwise, it is not.

• If the proof is valid, TPA will send a positive report to the user. Otherwise, a negative report will be sent instead.

8) Open: When users have performed malicious actions on the shared data, at least t GMs work together to trace the real identity of the group user as follows:

• Negotiate with each other to construct a polynomial $y(x) = \sum_{l=1}^t f(l) \cdot F_l(x) = \sum_{l=1}^t X(l) \cdot F_l(x)$, where the Lagrange polynomial interpolation $F_l(x) = \prod_{0 \leq h \leq t, h \neq l} (x-h) / (l-h)$.

• Compute the trace key $X = y(0) = \sum_{l=1}^t X(l) \cdot F_l(0)$.

• Compute $upk_i = T_{j,1} / T_{j,2}^X = A_i$, and then reveal the real identity of the signer through upk_i .

This procedure guarantees the current user can be found. When GMs need to find previous users who have affected the shared data, they can trace the data changes by implementing the post-order traversal to the additional binary tree, and then reveal the real user identities of each data change through the above procedure.

D. Discussions

1) Group Managers Dynamics:

• GM joining

If a new GM wants to join the group, the PKG computes $S' = S+1$, and tests whether $2t-1 \geq S'$. If it holds, the PKG will compute a new piece (S', X_s') with polynomial $f(x)$ and distribute it to

the new GM'S ; otherwise, the PKG chooses a new $(t' - 1)$ -degree polynomial $f'(x) = b'_0 + b'_1x + \dots + b'_{t'-1}x^{t'-1}$, where $2t' - 1 \geq S'$, $b'_0 = X$, $b'_1, \dots, b'_{t'-1} \in Z_q$, and computes $X'_l = f'(l) (l = 1, 2, \dots, S')$, i.e. X is divided into S' pieces X'_l and then distributed to GM_l .

In addition, the PKG generates a new key pair $\{spk', ssk'\}$, and broadcasts it to all the GMs, who can then share it with the existing group users. Note that the process of changing $\{spk, ssk\}$ has no effect on analysing, because the signing keys, the membership keys and the revocation keys of the existing users do not need to be changed. Nor do the signatures of the data blocks.

• GM leaving

If an existing GM_l wants to leave the group, the PKG first sets $S' = S - 1$, chooses a new $(t' - 1)$ -degree polynomial $f'(x) = b'_0 + b'_1x + \dots + b'_{t'-1}x^{t'-1}$, where $2t' - 1 \geq S'$, $b'_0 = X$, $b'_1, \dots, b'_{t'-1} \in Z_q$, and then computes and distributes new $X'_l = f'(l) (l = 1, 2, \dots, S')$ to each GM_l .

In addition, the PKG generates a new key pair $\{spk', ssk'\}$, and broadcasts it to all the GMs, who can then share it with the existing group users.

2) User Revocation: GMs maintain a

users-list, which is composed of each user's related key and expiration time. Once a user's service subscription expires, their signing key should become invalid from then on. In this case, by changing the membership information Ω and the key pair $\{spk, ssk\}$, any GM can instance the Revoke algorithm and putting the value of the revoked user's expiration time to be negative.

There might be misbehaving users in the group. In this case, any GM can invoke the Revoke algorithm as mentioned above. Note that when a user is revoked from a group, GMs do not need to re-compute and re-distribute new keys to the valid users, since the revoked user U_i cannot find $f, b \in Z_q$ such that $f \cdot u + b \cdot rvk_i = 1$, U_i cannot compute the partial signature V_2 any more.

If the revoked user U_i maliciously reveals their signing key $usk_i = (x_i, \pi)$, then the partial signature of other users can be discerned because of the common key π . However, it is not enough to forge a valid signature as the secret key x_j of the other users is still unknown. Therefore, the partial signature V_1 cannot be computed.

As we have demonstrated, valid users do not need to update their keys and the existing signatures. Signatures belonging to the revoked users can be re-computed by the GMs. Specifically, the existing user interacts with GMs to generate a proxy signature key, then GMs use the proxy key to compute the signatures of the revoked users. That transforms them into the signatures which sign by the private key of the existing user.

VI. EVALUATION

A. Functionality Comparison

Table II lists the features of NPP compared with other auditing schemes Knox and PDM for shared data in the cloud. As Table II shows, the two very important properties non-frameability and data traceability and recoverability are all not found in other two schemes. What's more, comparing to their schemes, NPP adds a lot of features. Hence, NPP has wider application than Knox and PDM.

B. Performance Analysis

In our experiments, we utilize Pairing Based Cryptography (PBC) library to simulate the cryptographic operations in

TABLE II
FUNCTIONALITY COMPARISON

	Knox [8]	PDM [19]	NPP
Public Auditing	Yes	Yes	Yes
Authorized Auditing	Yes	No	Yes
Identity Privacy	Yes	No	Yes
Traceability	Yes	No	Yes
Non-frameability	No	No	Yes
Data Traceability and Recoverability	No	No	Yes
User Revocation	No	Yes	Yes

TABLE III
COMMUNICATION COST COMPARISON

Scheme	Communication Cost(KB)
Knox [8]	$D w + (10D + k + 1) q + D(id + T) = 106.4$
PDM [19]	$(d + 5) q + D id = 4.6 + 0.02d$
NPP	$D w + (16D + 2) q + D id = 149.4$

TABLE IV
COMPUTATION COST COMPARISON

Scheme	Computation Cost(s)
Knox [8]	$D(2Exp_{Z_q} + 4Mul_{Z_q}) + kMul_{Z_q} + D(17Exp_{G_1} + 11Mul_{G_1}) + D(Exp_{G_T} + Mul_{G_T}) + 4Pair = 1.351$
PDM [19]	$(k + 6)Exp_{G_1} + (k + D + 3)Mul_{G_1} + (D + 3)Pair = 1.446$
NPP	$D(22Exp_{Z_q} + 14Mul_{Z_q}) + D(2Exp_{G_1} + 2Mul_{G_1}) + 2Pair = 0.236$

EXPZ_q and MULZ_q are one exponentiation operation and one multiplication operation on Z_q respectively; EXPG₁ and MULG₁ are one exponentiation operation and one multiplication operation

on Group G₁ respectively; EXPGT and MULGT are one exponentiation operation and one multiplication operation on Group GT respectively; Pair is a bilinear pairing operation.

the schemes. All tests are applied to a Ubuntu system with i7 3.40GHz-Intel Core and 4GB-memory over 1,000 times. We set the size of elements in G₁, G₂, G_T, Z_q as 160 bits (i.e., |q| = 160bit, |T| = 160bit), the identity of each data block as 50 bits (i.e., |id| = 50bit), and the number of the shared data blocks as 1,000,000 (i.e., w = 1,000,000 and |w| = 20bit). Each data block contains 100 elements (i.e., k = 100), the size of each data block is 2KB and the shared data is 2GB in all the experiments. Based on random sampling method [7], if the TPA select D = 460 data blocks, the detection probability is greater than 99%, and if D = 300, the detection probability is greater than 95%. To keep a higher detection probability, we chose D = 460. The performance analysis and the experiment results are as follows.

1) **Communication cost:** As Table III shows, the communication costs of NPP and Knox are both constant, but that of PDM linearly increases with the number of the group users. To support user revocation, NPP adds V₂ as a partial signature, which brings additional overhead |V₂| = 7D|q| = 62.89KB compared with Knox. However, compared with the shared data size of 2GB, the additional communication cost of 62.89KB is small and acceptable.

2) **Computation cost:** As Table IV shows, the computation costs of all the three schemes are constant, which are independent of the number of the group users. Obviously, NPP outperforms Knox and PDM. Because the operations on GT and the pairing operations are time-consuming, NPP has no operations on GT and has the fewest pairing operations. In contrast, Knox has several operations on GT and more pairing operations. Although the PDM has no operations on GT, the number of pairing operations in PDM linearly increase with D.

3) **Performance results:** From the above analysis, NPP has the lowest computation cost compared with Knox and PDM. Specifically, the computation cost of Knox is almost 5.7 times that of NPP, and PDM is almost 6.1 times that of NPP. Therefore, in terms of computation cost, NPP significantly outperforms Knox and PDM. As for communication cost, although the cost of NPP is a bit more than that of Knox, the additional overhead 63KB is small and acceptable compared to the size of shared data with 2GB.

VII. CONCLUSION

In this paper, we propose a novel multi-level privacy preserving public auditing scheme for cloud data sharing with multiple managers. During the process of auditing, the TPA cannot obtain the identities of the signers, which ensures the identity privacy of the group users. Moreover, unlike the existing schemes, the proposed NPP requires at least t group managers to work together to trace the identity of the misbehaving user. Therefore, it eliminates the abuse of single authority power and ensures non-frameability. Exceptionally, group users can trace the data changes through the designed binary tree and recover the latest correct data block when the current data block is damaged. In addition, the analysis and the experimental results show that NPP is provably secure and efficient.

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